

Saint Paul's Catholic Primary School

Hyde



Calculation Policy

St. Pauls Catholic Primary School - Calculation Policy

Addition

Stage 1

+ = signs and missing numbers

Children need to understand the concept of equality before using the "=" sign. Calculations should be written either side of the equality sign so the sign is not just interpreted as "the answer".

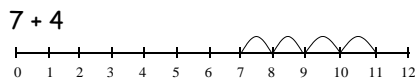
$$\begin{aligned} 2 &= 1 + 1 \\ 2 + 3 &= 4 + 1 \\ 3 &= 3 \\ 2 + 2 + 2 &= 4 + 2 \end{aligned}$$

Missing numbers need to be placed in all possible places.

$$\begin{array}{ccc} 3 + 4 & = & \triangle \\ 3 + \triangle & = & 7 \end{array} \quad \begin{array}{ccc} \triangle & = & 7 \\ + \triangle & = & \square \end{array}$$

Number lines

Use number lines to support the understanding of mental methods. Jumping in ones.



Stage 2

+ = signs and missing numbers

Continue using a range of equations as in stage 1 but with appropriate, larger numbers.

Extend to

$$14 + 5 = 10 + \square$$

and

$$32 + \square + \square = 100 \quad 35 = 1 + \square + 5$$

Partition into tens and ones and recombine

$$12 + 23 = 10 + 2 + 20 + 3$$

$$= 30 + 5$$

$$= 35$$

Count on in tens and ones

$$23 + 12 = 23 + 10 + 2$$

$$= 33 + 2$$

$$= 35$$

Partitioning and bridging through 10.

The steps in addition often bridge through a multiple of 10

e.g.

Children should be able to partition the 7 to relate adding the 2 and then the 5.

$$8 + 7 = 15$$

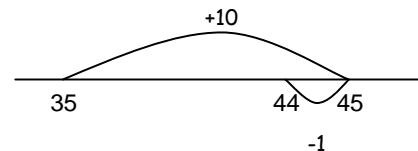


Add 9 or 11 by adding 10 and adjusting by 1

e.g.

Add 9 by adding 10 and adjusting by 1

$$35 + 9 = 44$$



Stage 3

+ = signs and missing numbers

Continue using a range of equations as in stages 1 and 2 but with appropriate, larger numbers.

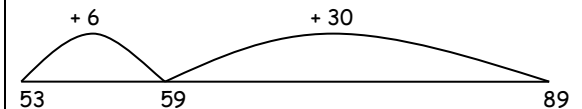
Partition into tens and ones

- Partition both numbers and recombine.
- Count on by partitioning the second number only e.g.

$$36 + 53 = 53 + 6 + 30$$

$$= 59 + 30$$

$$= 89$$



Add a near multiple of 10 to a two-digit number

Secure mental methods by using a number line to model the method. Continue as in stage 2 but with appropriate numbers

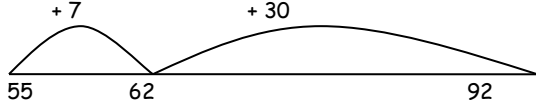
e.g. 35 + 19 is the same as 35 + 20 - 1.

Pencil and paper procedures

$$53 + 42 = 95 \text{ (no carrying)}$$

1 st	50 + 3	then	53	onto	53
	<u>40 + 2</u>		<u>42</u>		<u>42</u>
	90 + 5 = 95		5		<u>95</u>
			<u>90</u>		
			95		

St. Pauls Catholic Primary School - Calculation Policy

<u>Addition</u>		
Stage 4	Stage 5	Stage 6
<p><u>+ = signs and missing numbers</u> Continue using a range of equations as in stage 1 and 2 but with appropriate numbers.</p> <p><u>Partition into tens and ones and recombine</u> Either partition both numbers and recombine or partition the second number only e.g. $55 + 37 = 55 + 7 + 30$ $= 62 + 30$ $= 92$</p>  <p><u>Add the nearest multiple of 10, then adjust</u> Continue as in stage 2 and 3 but with appropriate numbers e.g. $63 + 29$ is the same as $63 + 30 - 1$</p> <p><u>Pencil and paper procedures</u> Single carry- 367 $\begin{array}{r} 367 \\ +251 \\ \hline 618 \\ 1 \end{array}$ Double carry- 367 $\begin{array}{r} 367 \\ +185 \\ \hline 552 \\ 11 \end{array}$ Leading onto using the carry one instead of partitioning.</p>	<p><u>+ = signs and missing numbers</u> Continue using a range of equations as in stage 1 and 2 but with appropriate numbers.</p> <p><u>Add or subtract the nearest multiple of 10 or 100, then adjust</u> Continue as in stages 2, 3 and 4 but with appropriate numbers e.g. $458 + 79 =$ is the same as $458 + 80 - 1$.</p> <p><u>Pencil and paper procedures</u> Extend to numbers with at least four digits $3587 + 675 = 4262$</p> <p>Treble carry- 3587 $\begin{array}{r} 3587 \\ + 675 \\ \hline 4262 \\ 111 \end{array}$</p> <p>Extend to up to two places of decimals (same number of decimals places) first without carrying any numbers, then with.</p> $\begin{array}{r} 72.8 \\ +54.6 \\ \hline 127.4 \\ 11 \end{array}$	<p><u>+ = signs and missing numbers</u> Continue using a range of equations as in stage 1 and 2 but with appropriate numbers.</p> <p><u>Add the nearest multiple of 10, 100 or 1000, then adjust</u> Continue as in stages 2, 3, 4 and 5 but with appropriate numbers including extending to adding 0.9, 1.9, 2.9 etc</p> <p><u>Pencil and paper procedures</u> Extend to numbers with any number of digits and decimals with 1, 2 and/or 3 decimal places and with a treble carry. $13.86 + 9.481 = 23.341$</p> $\begin{array}{r} 13.86 \\ + 9.481 \\ \hline 23.341 \\ 111 \end{array}$

St. Pauls Catholic Primary School - Calculation Policy

Subtraction

Stage 1

- = signs and missing numbers

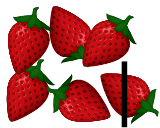
$$7 - 3 = \square \quad \square = 7 - 3$$

$$7 - \square = 4 \quad 4 = \square - 3$$

$$\square - 3 = 4 \quad 4 = 7 - \square$$

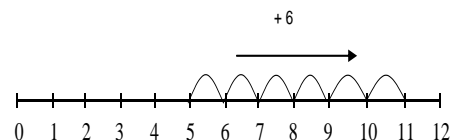
$$\square - \nabla = 4 \quad 4 = \square - \nabla$$

- Understand subtraction as 'take away'



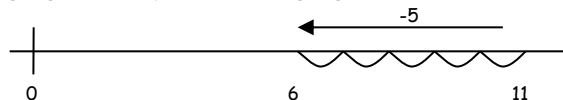
- Find a 'difference' by counting up;

I have saved 5p. The socks that I want to buy cost 11p. How much more do I need in order to buy the socks?



- Use practical and informal written methods to support the subtraction of a one-digit number from a one digit or two-digit number and a multiple of 10 from a two-digit number.

I have 11 toy cars. There are 5 cars too many to fit in the garage. How many cars fit in the garage?



Use the vocabulary related to addition and subtraction and symbols to describe and record addition and subtraction number sentences

Recording by

- drawing jumps on prepared lines
- constructing own lines

Stage 2

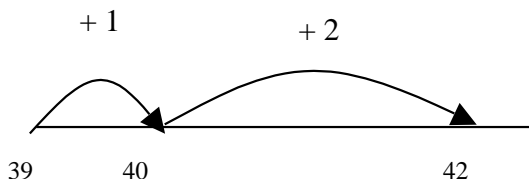
- = signs and missing numbers

Continue using a range of equations as in Stage 1 but with appropriate numbers.

Extend to $14 + 5 = 20 - \square$

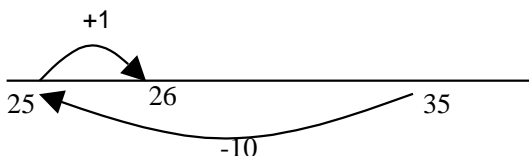
Find a small difference by counting up

$$42 - 39 = 3$$



Subtract 9 or 11. Begin to add/subtract 19 or 21

$$35 - 9 = 26$$



Use known number facts and place value to subtract

(partition second number only)

$$37 - 12 = 37 - 2 = 35$$

$$35 - 10 = 25$$

Stage 3

- = signs and missing numbers

Continue using a range of equations as in Stage 1 and 2 but with appropriate numbers.

Find a small difference by counting up

Continue as in Stage 2 but with appropriate numbers
e.g. $102 - 97 = 5$

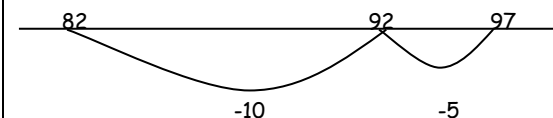
Subtract mentally a 'near multiple of 10' to or from a two-digit number

Continue as in Stage 2 but with appropriate numbers
e.g. $78 - 49$ is the same as $78 - 50 + 1$

Use known number facts and place value to subtract

Continue as in Stage 2 but with appropriate numbers
e.g.

$$97 - 15 = 82$$



With practice, children will need to record less information and decide whether to count back or forward. It is useful to ask children whether counting up or back is the more efficient for calculations such as $57 - 12$, $86 - 77$ or $43 - 28$.

St. Pauls Catholic Primary School - Calculation Policy

Subtraction

Stage 4

- = signs and missing numbers

Continue using a range of equations as in Stage 1 and 2 but with appropriate numbers.

Find a small difference by counting up

e.g. $5003 - 4996 = 7$

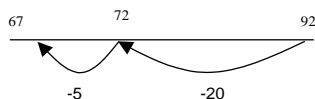
This can be modelled on an empty number line (see complementary addition below). Children should be encouraged to use known number facts to reduce the number of steps.

Subtract the nearest multiple of 10, then adjust.

Continue as in Stage 2 and 3 but with appropriate numbers.

Use known number facts and place value to subtract

$$92 - 25 = 67$$



Pencil and paper procedures

$$\begin{array}{r} \text{No carry (TU-TU)} \quad 367 \\ -251 \\ \hline 116 \end{array}$$

$$\begin{array}{r} \text{No carry (HTU-HTU)} \quad 387 \\ -173 \\ \hline 214 \end{array}$$

Stage 5

- = signs and missing numbers

Continue using a range of equations as in Stage 1 and 2 but with appropriate numbers.

Find a difference by counting up

e.g. $8006 - 2993 = 5013$

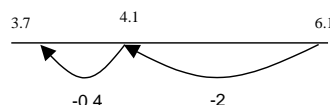
This can be modelled on an empty number line (see complementary addition below).

Subtract the nearest multiple of 10 or 100, then adjust.

Continue as in Stage 2, 3 and 4 but with appropriate numbers.

Use known number facts and place value to subtract

$$6.1 - 2.4 = 3.7$$



Pencil and paper procedures

Decimals that line up

$$\begin{array}{r} 14.65 \\ -12.41 \\ \hline 2.24 \end{array}$$

Single Carry

$$\begin{array}{r} 2 \quad 16 \\ 367 \\ -271 \\ \hline 96 \end{array}$$

Double Carry

$$\begin{array}{r} 2 \ 15 \ 12 \\ 362 \\ -275 \\ \hline 87 \end{array}$$

Stage 6

- = signs and missing numbers

Continue using a range of equations as in Stage 1 and 2 but with appropriate numbers.

Find a difference by counting up

e.g. $8000 - 2785 = 5215$

To make this method more efficient, the number of steps should be reduced to a minimum through children knowing:

- Complements to 1, involving decimals to two decimal places ($0.16 + 0.84$)
- Complements to 10, 100 and 1000

Subtract the nearest multiple of 10, 100 or 1000,
then adjust

Continue as in Stage 2, 3, 4 and 5 but with appropriate numbers.

Pencil and paper procedures


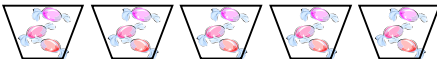
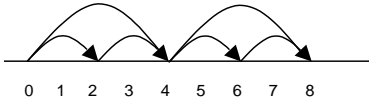

Subtractions that don't line up

$$\begin{array}{r} 5 \text{ } 11 \\ 2761 \\ - 247 \\ \hline 2514 \end{array}$$

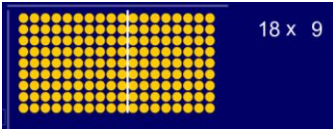
Decimals that don't line up	$ \begin{array}{r} 15.96 \\ - 7.62 \\ \hline 8.34 \end{array} $
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$$\begin{array}{r} 5 \ 11 \ 12 \ 17 \\ \text{Treble Carry (4 digits)} \\ 6237 \\ -4379 \\ \hline 1658 \end{array}$$



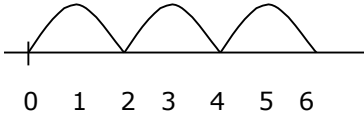

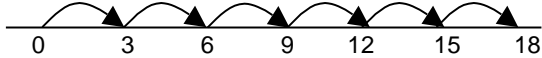
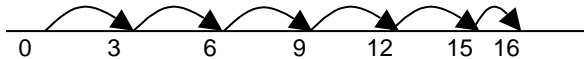
St. Pauls Catholic Primary School - Calculation Policy

Multiplication																														
Stage 1	Stage 2	Stage 3																												
<p>Multiplication is related to doubling and counting groups of the same size.</p> <div></div> <div><div>Looking at columns 2 + 2 + 2 3 groups of 2</div><div>Looking at rows 3 + 3 2 groups of 3</div></div> <p><u>Counting using a variety of practical resources</u> Counting in 2s e.g. counting socks, shoes, animal's legs... Counting in 5s e.g. counting fingers, fingers in gloves, toes... Counting in 10s e.g. fingers, toes...</p> <p><u>Pictures / marks</u></p> <p>There are 3 sweets in one bag. How many sweets are there in 5 bags?</p> <div></div>	<p><u>x = signs and missing numbers</u> 7 x 2 = □ □ = 2 x 7 7 x □ = 14 14 = □ x 7 □ x 2 = 14 14 = 2 x □ □ x ▽ = 14 14 = □ x ▽</p> <p><u>Arrays and repeated addition</u></p> <div><div><div><div>•</div><div>•</div><div>•</div><div>•</div></div><div><div>•</div><div>•</div><div>•</div><div>•</div></div></div><div>4 x 2 or 4 + 4</div></div> <div><div>2 x 4 or 2 + 2 + 2 + 2</div><div></div></div> <p><u>Doubling multiples of 5 up to 50</u> 15 x 2 = 30</p> <p><u>Partition</u> Children need to be secure with partitioning numbers into 10s and 1s and partitioning in different ways: 6 = 5 + 1 so e.g. Double 6 is the same as double five add double one.</p> <div><div></div><div><p>then</p><table><tr><td>X</td><td>10</td><td>5</td><td></td></tr><tr><td>2</td><td>20</td><td>10</td><td>= 30</td></tr></table></div></div>	X	10	5		2	20	10	= 30	<p><u>x = signs and missing numbers</u> Continue using a range of equations as in Stage 2 but with appropriate numbers.</p> <p><u>Arrays and repeated addition</u> Continue to understand multiplication as repeated addition and continue to use arrays (as in Stage 2).</p> <p><u>Doubling multiples of 5 up to 50</u> 35 x 2 = 70</p> <p><u>Partition</u></p> <table><tr><td>X</td><td>30</td><td>5</td><td></td></tr><tr><td>2</td><td>60</td><td>10</td><td>= 70</td></tr></table> <p>Use known facts and place value to carry out simple multiplications</p> <p>Use the same method as above (partitioning), e.g.</p> <p>32 x 3 = 96</p> <table><tr><td>x</td><td>30</td><td>2</td><td></td></tr><tr><td>3</td><td>90</td><td>6</td><td></td></tr><tr><td></td><td></td><td></td><td>= 96</td></tr></table>	X	30	5		2	60	10	= 70	x	30	2		3	90	6					= 96
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St. Pauls Catholic Primary School - Calculation Policy

<u>Multiplication</u>																																					
Stage 4	Stage 5	Stage 6																																			
<u>x = signs and missing numbers</u> Continue using a range of equations as in Year 2 but with appropriate numbers <u>Partition</u> Continue to use arrays:  $18 \times 9 = 162$ $18 \times 9 = (10 \times 9) + (8 \times 9) = 162$ OR Use the grid method of multiplication (as below) <u>Pencil and paper procedures</u> Grid method 23×7 is approximately $20 \times 10 = 200$ <table><tr><td>x</td><td>20</td><td>3</td><td></td><td>and</td><td>23</td></tr><tr><td>7</td><td>140</td><td>21</td><td>= 161</td><td></td><td>$\begin{array}{r} \times 7 \\ 23 \\ \hline 161 \end{array}$</td></tr></table>	x	20	3		and	23	7	140	21	= 161		$\begin{array}{r} \times 7 \\ 23 \\ \hline 161 \end{array}$	<u>x = signs and missing numbers</u> Continue using a range of equations as in Year 2 but with appropriate numbers <u>Partition</u> $47 \times 6 = 282$ $47 \times 6 = (40 \times 6) + (7 \times 6) = 282$ OR Use the grid method of multiplication (as below) <u>Pencil and paper procedures</u> Grid method 72×38 is approximately $70 \times 40 = 2800$ <table><tr><td>X</td><td>70</td><td>2</td></tr><tr><td>30</td><td>2100</td><td>60 = 2160</td></tr><tr><td>8</td><td>560</td><td>16 = 576</td></tr><tr><td></td><td></td><td>2736</td></tr></table> And <table><tr><td>$\begin{array}{r} 72 \\ \times 38 \\ \hline 2100 \\ 560 \\ 60 \\ 16 \\ \hline 2736 \end{array}$</td></tr></table> Extend to simple decimals with one and two decimal place.	X	70	2	30	2100	60 = 2160	8	560	16 = 576			2736	$\begin{array}{r} 72 \\ \times 38 \\ \hline 2100 \\ 560 \\ 60 \\ 16 \\ \hline 2736 \end{array}$	<u>x = signs and missing numbers</u> Continue using a range of equations as in Year 2 but with appropriate numbers <u>Partition</u> $87 \times 6 = 522$ $87 \times 6 = (80 \times 6) + (7 \times 6) = 522$ <u>Pencil and paper procedures</u> Long Multiplication <table><tr><td></td><td>352</td></tr><tr><td>X 27</td><td></td></tr><tr><td></td><td>2464</td></tr><tr><td></td><td>7040</td></tr><tr><td></td><td><u>9504</u></td></tr></table>		352	X 27			2464		7040		<u>9504</u>
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St. Pauls Catholic Primary School - Calculation Policy

Division		
Stage 1	Stage 2	Stage 3
<p><u>Sharing</u></p> <p>Requires secure counting skills</p> <p>-see counting and understanding number strand</p> <p>Develops importance of one-to-one correspondence</p> <p>See appendix for additional information on x and ÷ and aspects of number</p> <p>Sharing - 6 sweets are shared between 2 people. How many do they have each?</p>  <p>Practical activities involving sharing, distributing cards when playing a game, putting objects onto plates, into cups, hoops etc.</p> <p><u>Grouping</u></p> <p>Sorting objects into 2s / 3s/ 4s etc</p> <p>How many pairs of socks are there?</p>  <p>There are 12 crocus bulbs. Plant 3 in each pot. How many pots are there?</p> <p>Jo has 12 Lego wheels. How many cars can she make?</p>	<p><u>÷ = signs and missing numbers</u></p> <p>$6 \div 2 = \square$ $\square = 6 \div 2$</p> <p>$6 \div \square = 3$ $3 = 6 \div \square$</p> <p>$\square \div 2 = 3$ $3 = \square \div 2$</p> <p>$\square \div \nabla = 3$ $3 = \square \div \nabla$</p> <p><u>Grouping</u></p> <p>Link to counting and understanding number strand</p> <p>Count up to 100 objects by grouping them and counting in tens, fives or twos;...</p> <p>Find one half, one quarter and three quarters of shapes and sets of objects</p> <p>$6 \div 2$ can be modelled as:</p> <p>There are 6 strawberries.</p> <p>How many people can have 2 each? How many 2s make 6?</p> <p>$6 \div 2$ can be modelled as:</p>  <p>In the context of money count forwards and backwards using 2p, 5p and 10p coins</p> <p>Practical grouping e.g. in PE</p> <p>12 children get into teams of 4 to play a game. How many teams are there?</p> 	<p><u>÷ = signs and missing numbers</u></p> <p>Continue using a range of equations as in Stage 2 but with appropriate numbers.</p> <p><u>Understand division as sharing and grouping</u></p> <p>$18 \div 3$ can be modelled as:</p> <p>Sharing - 18 shared between 3 (see Stage 1 diagram)</p> <p>OR</p> <p>Grouping - How many 3's make 18?</p>  <p><u>Remainders</u></p> <p>$16 \div 3 = 5 \text{ r}1$</p> <p>Sharing - 16 shared between 3, how many left over?</p> <p>Grouping - How many 3's make 16, how many left over?</p> <p>e.g.</p> 

St. Pauls Catholic Primary School - Calculation Policy

Division

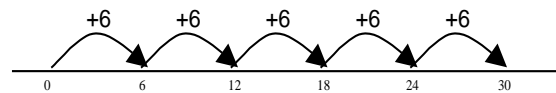
Stage 4

÷ = signs and missing numbers

Continue using a range of equations as in Stage 2 but with appropriate numbers.

Sharing and grouping

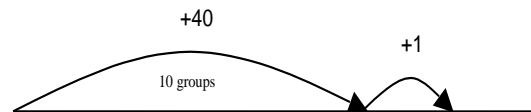
$30 \div 6$ can be modelled as:
grouping - groups of 6 placed on no. line and the number of groups counted e.g.



sharing - sharing among 6, the number given to each person

Remainders

$$41 \div 4 = 10 \text{ r}1$$



$$41 = (10 \times 4) + 1$$

Stage 5

÷ = signs and missing numbers

Continue using a range of equations as in Stage 2 but with appropriate numbers.

Sharing and grouping

Continue to understand division as both sharing and grouping (repeated subtraction).

Pencil and paper procedures

$196 \div 6$ is approximately just over $180 \div 6 = 30$

Short division (HTU \div U)

$$\begin{array}{r} 196 \div 6 \\ \underline{32 \text{ r } 4} \\ 6 \sqrt{196} \end{array}$$

Stage 6

÷ = signs and missing numbers

Continue using a range of equations as in Stage 2 but with appropriate numbers.

Sharing and grouping

Continue to understand division as both sharing and grouping (repeated subtraction).

Pencil and paper procedures

$434 \div 14$ is nearly $450 \div 15 = 30$

Long division (HTU \div TU)

$$\begin{array}{r} \underline{31} \\ 14 \overline{) 434} \\ \underline{-42} \downarrow \\ 14 \\ \underline{-14} \\ 0 \end{array}$$